

<u>Title</u>

```
svarih bfanelli — Heteroskedasticity-identified SVAR models,
Bacchiocchi/Fanelli (2012) methodology
```

<u>Syntax</u>

svarih bfanelli depvarlist [if] [in] , rgmvar(rgmvarname)
 [optional_options]

options	Description
Model: IH part	
rgmvar(rgmvarname)	identify regimes by contents of variable <i>rgmvarname</i>
<pre>bconstraints(constraints_b)</pre>	apply previously defined <i>constraints_b</i> to B
beq(matrix_beq)	define and apply to B equality constraint matrix matrix beg
<pre>bcns(matrix_bcns)</pre>	define and apply to B cross-parameter constraint matrix <i>matrix bcns</i>
<pre><u>e#con</u>straints(constraints_e#)</pre>	apply previously defined <i>constraints_e#</i> to E# . for 2 < # < 4
<u>e#e</u>q(matrix_e#eq)	define and apply to E# equality constraint matrix matrix_e#eq, for 2 ≤ # < 4
e#cns(matrix_e#cns)	<pre>define and apply to E# cross-parameter constraint matrix matrix_e#cns, for 2 ≤ # < 4</pre>
<u>noiden</u> check	do not check for local identification
<pre>Model: VAR part lags(numlist) exog(varlist exog) noconstant dfk small</pre>	use lags <i>numlist</i> in the underlying VAR use exogenous variables varlist_exog suppress constant term make small-sample degrees-of-freedom adjustment report small-sample t and F statistics
Reporting and screen output <u>level(#)</u> var <u>nocnsreport</u> <u>notable</u> <u>display options</u>	set confidence level display underlying var output do not display constraints do not display estimation results table control column formats
Maximization evalmode(modenum) <u>maximize options</u>	choose between d0, d1, and d2 evaluators; rarely used control the maximization process
<u>coefl</u> egend	display legend instead of statistics

You must **tsset** your data before using **svarih bfanelli**; see <u>[TS] tsset</u>. *varlist_exog* may contain time-series operators; see <u>tsvarlist</u>. *depvarlist* may NOT contain time-series operators. See <u>svarih postestimation</u> for features available after estimation.

Description

svarih bfanelli provides an alternative identification scheme for structural VARs than those implemented in <u>svar</u>. It implements a variant of the the "Identification through Heteroskedasticity" (IH) method as put forth in <u>Bacchiocchi/Fanelli (2012)</u>. Differently than <u>svarih bacchiocchi</u> and <u>svarih <u>llutkepohl</u>, it does not assume stability of the VAR parameters across volatility regimes. For details of the model setup, see the <u>Remarks</u> section. For general information on IH methods and for other IH methods that are available, see svarih.</u>

Abbreviations, definitions, notation

This help entry uses abbreviations and definitions from svarih.

<u>Options</u>

→ Model: IH part └

rgmvar(*rgmvarname*) determines the variable whose observations identify the volatility regimes. It must be a numeric variable holding non-negative integer values between 1 and 4 where each integer value identifies a particular volatility regime.

Differently than <u>svarih bacchiocchi</u>, the regime encoding for **svarih bfanelli** is hardcoded in the following way: The baseline state (shock impact matrix B) is encoded by <u>rgmvar=1</u>. Its constraints are defined by options **bconstraints()**, **beq()**, and **bcns()**. There must be at least another volatility regime in the sample, represented by the paramter matrix E2. Its constraints are defined by options **e2constraints()**, **e2eq()**, and **e2cns()**. This state is encoded by <u>rgmvar=2</u>. There can be up to two additional volatility regimes in the model, represented by the paramter matrices E3 and E4. The constraint specification and the regime encoding is done in an analogous fashion to the second volatility state and uses integers 3 and 4.

In any model specification, the volatility encodings that occur in the sample must be contiguous. For example, you cannot estimate a model whose *rgmvar* has values 1, 2, and 4 in the estimation sample. If you want to run this specification, you need to recode *rgmvar* or generate a different *rgmvar* that carries encodings 1, 2, and 3.

Such a situation can occur if you restrict the estimation sample through the $[\underline{if}]$ $[\underline{in}]$ conditions. Assume that you have data for 1970ml-1999ml2 and variable **year** holds the year of observations. You define regimes such that rgmvar=1,2,3 for observations in the 70s, 80s, 90s, respectively. After defining sufficient constraints you can estimate the model for the entire sample and pass the local identification check. However, if you want to exclude the 80s from the sample by typing

. svarih bfa (...) if !inrange(year,1980,1989) (...)

you will receive an error, since *rgmvar* only holds values 1 and 3 in the restricted estimation sample, which are not contiguous. The solution is to generate a different *rgmvar* with state 3 recoded to 2, and using **e2** constraint options rather than **e3** constraint options.

Despite these limitations, the following still holds true: It is not a requirement that a particular regime has contiguous observations in time. There can be data gaps within a regime and between regimes. The sequence of regimes and the number of occurrences of one particular regime is unrestricted. For example, a regime sequence 2, 4, ., 4, 1, ., 3 can be accommodated by **svarih bfanelli** (a dot indicates missing values for *rgmvar* or data gaps).

bconstraints(constraints_b), beq(matrix_beq), bcns(matrix_bcns) have the same meaning and can be specified in a similar manner as bconstraints, beq, bcns in svar. See the exposition there. They define linear constraints on the baseline state shock impact matrix B. A difference to svar is that bconstraints() does accept restrictions across model matrices B, E2, E3 and E4.

beq(matrix_beq) defines equality constraints. matrix_beq usually is an existing matrix but it may also be an expression as in <u>matrix input</u> or a simple matrix function. For example, $beq((.,0\backslash.,.))$ and beq(I(2)) are allowed

bcns(*matrix_bcns*) defines cross-equation constraints. Argument *matrix_bcns* can be supplied in the same way as *matrix_beq* from option **beq()**.

bconstraints(constraints_b) can define either one. They are defined using the <u>constraint</u> command.

- e#constraints(constraints_e#), e#eq(matrix_e#eq), e#cns(matrix_e#cns), where #
 must be an integer in the range 2 ≤ # ≤ 4, work in the same way as
 bconstraints, beq and bcns. The define linear constraints on the shock
 impact modification matrices E2, E3, and E4.
- **noidencheck** skips the check for local identification of parameters. The check consists of examining the rank of a matrix at the parameter estimates. Full rank of this matrix is needed for identification. For details, see the associated PDF document to **svarih** or the working paper by <u>Bacchiocchi/Fanelli (2012)</u>.

____ Model: VAR part

lags(numlist) see <u>var</u> / <u>svar</u>.

exog(varlist_exog) see var / svar.

noconstant; see [R] estimation options.

dfk see var / svar.

small see <u>var</u> / <u>svar</u>.

level(#); see [R] estimation options.

var specifies that the output from var also be displayed. Note that there are multiple VARs underlying svarih bfanelli. By default, these VARs are fit quietly. This option is not available when you replay estimates.

nocnsreport; see [R] estimation options.

notable does not display the estimation output table.

display_options: cformat(%fmt), pformat(%fmt), and sformat(%fmt); see [R]
 estimation options.

Maximization

- evalmode(modenum) will choose between d0, d1, and d2 evaluators. Rarely used. The default is 2. Can be used to check the numerical robustness of large models.
- maximize_options: difficult, technique(algorithm spec), iterate(#), [no]log, trace, gradient, showstep, hessian, showtolerance, tolerance(#), ltolerance(#), nrtolerance(#), nonrtolerance(#), and from(init_specs); see [R] maximize.

coeflegend; see [R] estimation options.

<u>Remarks</u>

svarih bfanelli implements the IH-BFA method within a maximum likelihood framework as an extended SVAR B-model. The extension consists of positing a priori knowledge about different regimes of volatility, i.e. time periods during which the structural shocks have different variances and possibly nonzero covariances. Consequently, a prerequisite for estimation is the specification of a variable that identifies these regimes, which in the following is referred to as the "regime variable". The distinguishing feature of IH-BFA within the class of SVAR-IH methods is that it does not assume constancy of the VAR model parameters across regimes.

In terms of a typical structural VAR equation that relates VAR residuals u_t to structural shocks e_t, the model in Baccchiocchi/Fanelli (2012) reads

(1a) u_t = B*e_t , t is in regime 1
(1b) u_t = (B+E2)*e_t , t is in regime 2
(1c) u_t = (B+E3)*e_t , t is in regime 3
(1d) u_t = (B+E4)*e_t , t is in regime 4

As usual, B models the contemporaneous impact of shocks. E2, E3, and E4 model the volatility differentials between regimes 1 and 2, 3, 4.

Note that even if all E# matrices in the model are constrained to null matrices, (1a)-(1d) do not collapse into a standard SVAR B-model implemented in <u>svar</u> since each regime has its own separate underlying VAR regressions.

<u>Examples</u>

The following example illustrates the mechanics of IH-BFA. It does not discuss the important issues of the interpretation of the shocks. It focuses on the mechanics. It leans on the example given in **svar** so you can compare the **svarih bfa** setup to the one of **svar**.

Throughout this example section, we store estimated results in Stata's estimation results catalogue for later access. The utility <u>svarih examples</u> allows you to easily re-generate these estimates at any point.

In order to apply IH-BFA, we first must define a regime variable. To that end, we make the following assumptions: We have prior knowledge that the volatilities of the shocks in our model have changed in the 1970s. In addition, we have evidence that slope coefficients of the underlying VAR also have changed at the same time. We fix a date of regime change for 1974q1. The statement below generates a variable that contains values 1 and 2, as required by a **svarih bfa** model with two regimes.

. webuse lutkepohl2
. gen byte rgmvar = (gtr>=tg(1974g1)) + 1

It is worth reiterating that the occurence of regimes can be modeled to be much more complicated than this. Any sequence and any multiplicity of regimes, with any occurence of gaps in the data, are allowed. If there are enough observations, **svarih bfa** will produce estimates.

Before estimation, we have to decide which constraints we impose. Let's start with a lower triangular shock impact matrix in both regimes.

To illustrate the relation of IH-BFA to SVAR models, we run two subsample SVARs, one for each regime.

. matrix aeg = I(3)
. svar dln inv dln inc dln consump if rgmvar==1, aeg(aeg) beg(beg)
. est store bfa svar1
. svar dln inv dln inc dln consump if rgmvar==2, aeg(aeg) beg(beg)
. est store bfa svar2

The **svarih bfa** B-matrix estimates are identical to the **svar** B-matrix estimates for the regime 1 subsample. The sum of the **svarih bfa** B and E-matrix estimates corresponds to the **svar** B-matrix estimates for the regime 2 subsample. We compare the first subsample:

. estimates table bfa svarrepl bfa svar1 , p stats(ll N)

To confirm the second claim we take advantage of the replay functionality of **svarih** invoked by the option **cmat**.

. estimates restore bfa_svarrepl . svarih, cmat bpluse(2) format(%12.4f) . estimates replay bfa_svar2 , nocnsreport

So far, there is nothing gained in comparison to SVAR models. IH-BFA, However, can achieve identification schemes not possible in SVAR models. Below we relax the restriction on element B[1,2], but add some more restrictions to E2: The resulting scheme allows for a differential impact of the first shock on the first two endogenous variables in regime 2, and of the second shock on the second model variable.

In order to perform a LR-test to test whether the two differential impacts on the second endogenous variable can be excluded, we estimate a constrained model:

. matrix e2eq = (.,0,0 \ 0,0,0 \ 0,0,0)
. svarih bfa dln inv dln inc dln consump , rgmvar(rgmvar) e2eq(e2eq)
 beq(beq)
. est store bfa constr
. lrtest bfa constr bfa unconstr , stat

The exclusion restrictions cannot be rejected at any conventional level.

predict after **svarih bfanelli** generates prediced values, residuals, shocks, and historical decompositions. **dsimih** generates dynamic simulation statistics. For all features available after estimation, see <u>svarih postestimation</u>.

Saved results

svarih bfanelli saves the following in e():

Scalars number of observations e(N) e(N_cns) number of constraints number of equations in **e(b)** e(k_eq) e(k_dv) number of dependent variables number of auxiliary parameters e(k_aux) e(ll) log likelihood e(N_var#) number of observations for VAR # e(N_gaps_var#) number of gaps in the sample for underlying VAR #e(k_var) number of coefficients in each underlying VAR number of equations in each underlying VAR e(k_eq_var) e(k_dv_var) number of dependent variables in each underlying VAR e(df_eq_var) average number of parameters in an equation of each underlying VAR e(df_r_var#) if small, VAR residual degrees of freedom for VAR # e(mlag) highest lag in VAR e(tmin_var#) first time period in the sample for VAR # e(tmax_var) maximum time for VAR # rank of e(V) e(rank) e(ic_ml) number of ML iterations return code from **ml** e(rc_ml) e(converged_ml) 1 if ml declared convergence, 0 otherwise e(numregimes) number of regimes marked by regimevar

Macros	
e(cmd)	svarih
e(method)	BFanelli
e(version)	version number of command
e(cmdline)	command as typed
e(lags)	lags in model
e(depvar)	names of dependent variables
e(rgmvar)	name of variable that identifies regimes
e(exog)	names of exogenous variables, if specified
e(nocons)	noconstant, if noconstant specified
e(cns_b)	comprehensive list of constraints on B
e(cns e#)	comprehensive list of constraints on E#
e(dfk var)	alternate divisor (dfk), if specified
e(small)	small, if specified
e(tsfmt)	format of timevar
e(timevar)	name of timevar
e(title)	title in estimation output
e(predict)	program used to implement predict
e(from)	contents of maximization option from , if specified as a
	string
e(mlopts)	maximization options used
e(idencheck)	result of identification check; one of passed, failed, or
	skipped
e(regimes)	regime encodings that occur in sample
e(regimes Ns)	number of observations in each regime
-	_
Matrices	
e(b)	coefficient vector
e(Cns)	constraints matrix
e(Sigma_var#)	Residual covariance matrix for underlying VAR #
e(V)	variance-covariance matrix of the estimators
e(b_var#)	coefficient vector for underlying VAR #
e(V_var#)	VCE for underlying VAR #
e(beq)	beq(matrix) , if specified
e(bcns)	<pre>bcns(matrix), if specified</pre>
e(e#eq)	e#eq(matrix), if specified
e(e#cns)	e#cns(<i>matrix</i>) , if specified
e(B)	estimated B matrix
e(E#)	estimated E# matrix
e(from)	matrix of maximization option from , if specified as a
	matrix
Functions	
e(sample)	marks estimation sample

<u>Author</u>

Daniel C. Schneider, Goethe University Frankfurt, dan_schneider@outlook.com

Acknowledgements

The code of official Stata's **svar** has served as a point of reference throughout the development of **svarih bfanelli**. Any remaining errors in **svarih bfanelli** are mine.

<u>References</u>

Bacchiocchi, E. and L. Fanelli (2012): Identification in Structural Vector Autoregressive Models with Structural Changes. Universita Degli Studi di Milano, Working Paper No.2012-16.

<u>Also see</u>